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Paper Participant

Gede Rasben Dantes

- Doctoral Student in Computer Science Department, University of Indonesia

Widodo Budiharto, DjokoPurwanto, Mauridhi Hery Purnomo

- Electrical Engineering Department Institut Teknologi Surabaya

Untung Rahardja, Valent

- STMIK RAHARJA Raharja Enrichment Centre (REC)
Tangerang - Banten, Republic of Indonesia

Diyah Puspitaningrum, Henderi

- Information System, Faculty of Computer Science

Wiwik Anggraeni, Danang Febrian

- Information System Department, Institut Teknologi Sepuluh Nopember

Aan Kurniawan, Zainal A. Hasibuan

- Faculty of Computer Science, University of Indonesia

Untung Rahardja, Edi Dwinarko, Muhamad Yusup

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia
- GADJAH MADA UNIVERSITY Faculty of Mathematics and Natural Sciences Yogyakarta,

Sarwosri, Djiwandou Agung Sudiyono Putro

- Department of Informatics, Faculty of Information Technology
- Institute of Technology Sepuluh Nopember

Chastine Fatichah, Nurina Indah Kemalasari

- Department, Faculty of Information Technology
- Institut Teknologi Sepuluh Nopember, Kampus ITS Surabaya

Untung Rahardja, Jazi Eko Istiyanto

- STMIK RAHARJA Raharja Enrichment Centre (REC)
Tangerang - Banten, Republic of Indonesia
- GADJAH MADA UNIVERSITY Yogyakarta, Republic of Indonesia

Bilqis Amaliah, Chastine Fatichah, Diah Arianti

- Informatics Department – Faculty of Technology Information
- Institut Teknologi Sepuluh Nopember (ITS), Surabaya, Indonesia

Tri Pujadi

- Information System Department – Faculty of Computer Study Universitas Bina Nusantara
Jl. Kebon Jeruk Raya No. 27, Jakarta Barat 11530 Indonesia

Untung Rahardja, Retantyo Wardoyo, Shakinah Badar

- Faculty of Information System, Raharja University Tangerang, Indonesia
- Faculty of Mathematics and Natural Science, Gadjah Mada University Yogyakarta, Indonesia
- Faculty of Information System, Raharja University Tangerang, Indonesia

Paper Participant

Henderi, Maimunah, Asep Saefullah

- Information Technology Department – Faculty of Computer Study STMIK Raharja
Jl. Jenderal Sudirman No. 40, Tangerang 15117 Indonesia

Yeni Nuaraeni

- Program Study Information Technology University Paramadina

Sfenrianto

- Doctoral Program Student in Computer Science University of Indonesia

Asep Saefullah, Sugeng Santoso

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia

Henderi, Maimunah, Aris Martono

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia

M. Tajuddin, Zainal Hasibuan, Abdul Manan, Nenet Natasudian, Jaya

- STMIK Bumigora Mataram West Nusa Tenggara
- Indonesia University
- PDE Office of Mataram City
- ABA Bumigora Mataram

Ermatita, Edi Dwinarko, Retantyo Wardoyo

- Information systems of Computer science Faculty Sriwijaya University
(Student of Doctoral Program Gadjah Mada university)
- Computer Science of Mathematics and Natural Sciences Faculty Gadjah Mada University

Junaidi, Sugeng Santoso, Euis Sitinur Aisyah

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia

Ermatita, Huda Ubaya, Dwiroso Indah

- Information systems of Computer science Faculty Sriwijaya University
(Student of Doctoral Program Gadjah Mada university)
- Computer Science Faculty of Sriwijaya University Palembang-Indonesia.

Mauritsius Tuga

- Jurusan Teknik Informatika Universitas Katolik Widya Mandira Kupang

Padeli, Sugeng Santoso

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia

M. Givi Efgivia, Safarudin, Al-Bahra L.B.

- Staf Pengajar STMIK Muhammadiyah Jakarta
- Staf Pengajar Fisika, FMIPA, UNHAS, Makassar
- Staf Pengajar STMIK Raharja, Tangerang

Primantara, Armanda C.C, Rahmat Budiarto, Tri Kuntoro P.

- School of Computer Sciences, Univeristi Sains Malaysia, Penang, Malaysia
- School of Computer Science, Gajah Mada University, Yogyakarta, Indonesia

Paper Participant

Hany Ferdinando, Handy Wicaksono, Darmawan Wangsadiharja

- Dept. of Electrical Engineering, Petra Christian University, Surabaya - Indonesia

Untung Rahardja, Hidayati

- STMIK RAHARJA Raharja Enrichment Centre (REC) Tangerang - Banten, Republic of Indonesia

Dina Fitria Murad, Mohammad Irsan

- STMIK RAHARJA Raharja Enrichment Centre (REC)
Tangerang - Banten, Republic of Indonesia

Asep Saefullaf, Augury El Rayeb

- STMIK RAHARJA Raharja Enrichment Centre (REC)
Tangerang - Banten, Republic of Indonesia

Richardus Eko Indrajit

- ABFI Institute, Perbanas

Azzemi Arifin, Young Chul Lee, Mohd. Fadzil Amiruddin, Suhandi Bujang, Salizul Jaafar, Noor Aisyah, Mohd. Akib

- AKIB#6#System Technology Program, Telekom Research & Development Sdn. Bhd., TMR&D
Innovation Centre, Lingkaran Teknokrat Timur, 63000 Cyberjaya, Selangor Darul Ehsan, MALAYSIA
Division of Marine Electronics and Communication Engineering, Mokpo National Maritime
University (MMU) 571 Chukkyo-dong, Mokpo, Jeonnam, KOREA 530-729

Sutrisno

- Departement of Mechanical and Industrial Engineering, Gadjah Mada University,
Jl. Grafika 2 Yogyakarta. 52281
- Faculty of Mathematics and Natural Sciences, Gadjah Mada University,
- Departement of Geodetical Engineering, Gadjah Mada University,

Saifuddin Azwar, Untung Raharja, Siti Julaeaha

- Faculty Psychology, Gadjah Mada University Yogyakarta, Indonesia
- Faculty of Information System Raharja University Tangerang, Indonesia

Henderi, Sugeng Widada, Euis Siti Nuraisyah

- Technology Department – Faculty of Computer Study STMIK Raharja
Jl. Jenderal Sudirman No. 40, Tangerang 15117 Indonesia



Panel of Reviewers

Abdul Hanan Abdullah, Prof.

Universiti Teknologi Malaysia

Arif Djunaidy, Prof.

*Sepuluh November Institute of Technology,
Indonesia*

Djoko Soetarno, Ph.D

STMIK Raharja, Indonesia

Edi Winarko, Ph.D

Gajah Mada University, Indonesia

E.S. Margianti, Prof.

Gunadarma University, Indonesia

Iping Supriyana, Dr.

Bandung University of Technology, Indonesia

Jazi Eko Istiyanto, Ph.D

Gajah Mada University, Indonesia

K.C. Chan, Prof.

University of Glasgow, United Kingdom

Marsudi W. Kisworo, Prof.

Swiss-German University, Indonesia

Rahmat Budiharto, Prof.

Universiti Sains Malaysia

Stephane Bressan, Prof.

National University of Singapore

Suryo Guritno, Prof

Gajah Mada University, Indonesia

Susanto Rahardja, Prof.

Nanyang Technological University, Singapore

T. Basaruddin, Prof.

University of Indonesia,

Thomas Hardjono, Prof.

MIT, USA

Untung Rahardja, M.T.I.

STMIK Raharja, Indonesia

Wisnu Prasetya, Prof.

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Y. Sutomo, Prof.

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Paper

Saturday, August 8, 2009

13:55 - 14:15

Room L-210

MINING QUERIES FASTER USING MINIMUM DESCRIPTION LENGTH PRINCIPLE

Diyah Puspitaningrum, Henderi

Department of Computing Science Universiteit Utrecht
 diyah@cs.uu.nl

Information Technology Department – Faculty of Computer Study STMIK Raharja
 Jl. Jenderal Sudirman No. 40, Tangerang 15117 Indonesia
 email: henderi@pribadiraharja.com

Abstract

Ever since the seminal paper by Imielinski and Mannila [8], inductive databases have been a constant theme in the mining literature. Operationally, an inductive database is a database in which models and patterns are first class citizens.

Having models and patterns in the database raises many interesting problems. One, which has received little attention so far, is the following: do the models and patterns that are stored help in computing new models and patterns? For example, if we have induced a classifier C from the database and we compute a query Q . Does knowing C speed up the induction of a new classifier on the result of Q ? In this paper we answer this problem positively for one specific class of models: the code tables induced by our Krimp algorithm. The Krimp algorithm was built using minimum description length (MDL) principle. In Krimp algorithm, if we have the code tables for all tables in the database, then we can approximate the code table induced by Krimp on the result of a query, using only these global code tables as candidates; that is, we do not have to mine for frequent item sets on the query result. Since Krimp is linear in the number of candidates and it reduces the set of frequent item sets by many orders of magnitude, this means that we can speed up the induction of code tables on query results by many orders of magnitude.

Keywords: Inductive Database, Frequent Item Sets, MDL

1. Introduction

Ever since the start of research in data mining, it has been clear that data mining, and more general the KDD process, should be merged into DBMSs. Since the seminal paper by Imielinski and Mannila [8], the so-called inductive databases have been a constant theme in data mining research.

Perhaps surprisingly, there is no formal definition of what an inductive database actually is. In fact, de Raedt in [12] states that it might be too early for such a definition. There is, however, consensus on some aspects of inductive databases. An important one is that models and patterns should be first class citizens in such a database. That is, e.g., one should be able to query for patterns.

Having models and patterns in the database raises interesting new problems. One, which has received little attention so far, is the following: do the models and patterns that are stored help in computing new models and patterns? For example, if we have induced a classifier C from the database and we compute a query Q . Does knowing C speed up the induction of a new classifier on the result of Q ?

In fact, this general question is not only interesting in the context of inductive databases, it is of prime importance in everyday data mining practice.

In the data mining literature, the usual assumption is that we are given some database that has to be mined.

In practice, however, this assumption is usually not met. Since the construction of the mining database is often one of the hardest parts of the KDD process. The data either resides in a data warehouse or in multiple databases, and the mining database is constructed from these underlying databases.

From most perspectives, it is not very interesting to know whether one of no importance whatsoever.

Intuitively, however, if the underlying databases contain one would hope that knowing such models would help in modelling the specially constructed 'mining database'. For example, if we have constructed a classifier on a database of customers, one would hope that this would help in developing a classifier for the female customers.

In this paper we study this problem for one specific class of databases, i.e., the code tables induced by our Krimp algorithm. Given all frequent item sets on a table, Krimp induces a small subset of these frequent item sets. The reason why we focus on Krimp is that together the selected item sets describe the underlying data distribution of the database very well, see, e.g., [14, 16].

In particular, we show that if we know the code tables induced by Krimp on the result of a query, using these item sets in these global code tables as candi-

dates linear in the number of candidates and Krimp induces a set of frequent item sets by many orders of magnitude smaller. This means that we can now speed up the induction of item sets on query results by many orders of magnitude. This results in a slightly less optimal code table, but it approximates the optimal solution within a few per cent. We formalise "approximation" in terms of MDL [7]. The data miner has a choice: either a quick, good approximation, or the optimal result taking longer time to compute.

The structure of this paper is as follows. In the next Section we formalise the general problem. Next, in Section 3 we give an introduction to our Krimp algorithm. In Section 4 we formalise the general problem in terms of Krimp. In Section 5 the experimental set-up is discussed. In Section 6 we discuss the experimental results, while in Section 7 we conclude.

In Section 8 we give an overview of related research. The conclusions and directions for further research are given in Section 9.

2. Preliminaries

In this section we start with some preliminaries and assumptions. We first formalise the problem informally. To

formalise it we use MDL, which is briefly discussed.

2.1 Preliminaries and Assumptions We assume that our data resides in relational databases. In fact, note that the union of two relational databases is, again, a relational database. Hence, we assume, without loss of generality, that our data resides in one relational database DB. So, the mining database is constructed from DB using queries. Given the compositionality of relational query languages, we may assume, again without loss of generality, that the analysis database is constructed using one query Q. That is, the analysis database is $Q(DB)$, for some relational algebra expression Q. Since DB is fixed, we will often simply write Q for $Q(DB)$; that is we will use Q to denote both the query and its result.

2.2 The Problem Informally In the introduction we stated that knowing a model on DB should help in inducing a model on Q. To make this more precise, let A be our data mining algorithm. A can be any algorithm, it may, e.g., compute a decision tree, all frequent item sets or a neural network. Let MDB denote the model induced by A from DB, i.e., $MDB = A(DB)$. Similarly, let $MQ = A(Q)$. We want to transform A into an algorithm A_{approx} that takes at least two inputs, i.e., both Q and MDB, such that:

1. A_{approx} gives a reasonable approximation of A when applied to Q, i.e., $A_{\text{approx}}(Q;MDB) \approx MQ$
2. $A_{\text{approx}}(Q;MDB)$ is simpler to compute than MQ. The second criterion is easy to formalise: the runtime of A_{approx} should be shorter than that of A. The first one is harder. What do we mean that one model is an approximation of another? Moreover, what does it mean that it is a reasonable approximation? There are many ways to formalise this. For example, for predictive models, one could use the difference between predictions as a way to measure how well one model approximates. While for clustering, one could use the number of pairs of points that end up in the same cluster.

We use the minimum description length (MDL) principle [7] to formalise the notion of approximation. MDL is quickly becoming a popular formalism in data mining research, see, e.g., [5] for an overview of other applications of MDL.

2.3 Minimum Description Length MDL like its close cousin MML (minimum message length) [17], is a practical version of Kolmogorov Complexity [11]. All three embrace the slogan Induction by Compression. For MDL, this principle can be roughly described as follows.

Given a set of models H , the best model $H^2 H$ is the one that minimizes $L(H) + L(D_j H)$ in which $L(H)$ is the length, in bits, of the description of H , and $L(D_j H)$ is the length, in bits, of the description of the data when encoded with H . One can paraphrase this by: the smaller $L(H) + L(D_j H)$, the better H models D .

What we are interested in is comparing two algorithms on the same data set, viz., on $Q(DB)$. Slightly abusing notation, we will write $L(A(Q))$ for $L(A(Q)) + L(Q(DB)jA(Q))$, similarly, we will write $L(A_{\text{Q;MDB}})$. Then, we are interested in comparing IMDL-theorists tend to talk about hypothesis in this context, hence the H ; see [7] for the details. $L(A_{\text{Q;MDB}})$ to $L(A(Q))$. The closer the former is to the latter, the better the approximation is. Just taking the difference of the two, however, can be quite misleading. Take, e.g., two databases $db1$ and $db2$ sampled from the same underlying distribution, such that $db1$ is far bigger than $db2$. Moreover, x a model H . Then necessarily $L(db1jH)$ is bigger than $L(db2jH)$.

In other words, big absolute numbers do not necessarily mean very much. We have to normalise the difference to get a feeling for how good the approximation is. Therefore we define the asymmetric dissimilarity measure (ADM) as follows. Definition 2.1. Let $H1$ and $H2$ be two models for a dataset D . The asymmetric dissimilarity measure $ADM(H1;H2)$ is defined by:
 $ADM(H1;H2) = jL(H1) - L(H2)j L(H2)$ Note that this dissimilarity measure is related to the Normalised Compression Distance. The reason why we use this asymmetric version is that we have a "gold standard". We want to know how far our approximate result $A_{\text{Q;MDB}}$ deviates from the optimal result $A(Q)$.

2.4 The Problem Before we can formalise our problem using the notation introduced above, we have one more question to answer: what is a reasonable approximation? For a large part the answer to this question is, of course, dependent on the application in mind. An ADM in the order of 10% might be perfectly alright in one application, while it is unacceptable in another.

Hence, rather than giving an absolute number, we make it into a parameter. Problem:

For a given data mining algorithm A , devise an algorithm A_{Q} , such that for all relational algebra expressions Q on a database DB :

1. $ADM(A_{\text{Q;MDB}};A(Q)) \ll$

2. Computing $A_{\text{Q;MDB}}$ is faster than computing $A(Q)$

2.5 A Concrete Instance: Krimp The ultimate solution to the problem as stated in above would be an algorithm that transforms any data mining algorithm A in an algorithm A_{Q} with the requested properties. This is a rather ambitious, ill-defined (what is the class of all data mining algorithms?), and, probably, not attainable goal. Hence, in this paper we take a more modest approach: we transform one algorithm only, our Krimp algorithm.

The reason for using Krimp as our problem instance is threefold. Firstly, from earlier research we know that Krimp characterises the underlying data distribution rather well; see, e.g., [14, 16]. Secondly, from earlier research on Krimp in a multi-relational setting, we already know that Krimp is easily transformed for joins [10]. Finally, Krimp is MDL based. So, notions such as $L(A(Q))$ are already defined for Krimp.

3. Introducing Krimp For the convenience of the reader we provide a brief introduction to Krimp in this section, it was originally introduced in [13] (although not by that name) and the reader is referred to that paper for more details.

Since Krimp selects a small set of representative item sets from the set of all frequent item sets, we first recall the basic notions of frequent item set mining [1].

3.1 Preliminaries Let $I = \{i_1, \dots, i_n\}$ be a set of binary (0/1 valued) attributes. That is, the domain D_i of item i is $\{0, 1\}$. A transaction (or tuple) over I is an element of $Q_i \{0, 1\}^n$. A database DB over I is a bag of tuples over I . This bag is indexed in the sense that we can talk about the i -th transaction. An item set J is, as usual, a subset of I , i.e., $J \subseteq I$. The item set J occurs in a transaction $t \in DB$ if $8I \in J: t(I) = 1$. The support of item set J in database DB is the number of transactions in DB in which J occurs. That is, $suppDB(J) = \{t \in DB \mid J \text{ occurs in } t\}$. An item set is called frequent if its support is larger than some user-defined threshold called the minimal support min-sup. Given the A Priori property, $8I \subseteq J: P(I) \subseteq J: suppDB(J) \geq min-sup$ frequent item sets can be mined efficiently level wise, see [1] for more details. Note that while we restrict ourselves to binary databases in the description of our problem and algorithms, this is a trivial generalisation to categorical databases. In the experiments, we use such categorical databases.

- 3.2 Krimp The key idea of the Krimp algorithm is the code table. A code table is a two-column table that has item sets on the left-hand side and a code for each item set on its right-hand side. The item sets in the code table

are ordered descending on 1) item set length and 2) support size and 3) lexicographically. The actual codes on the right-hand side are of no importance: their lengths are. To explain how these lengths are computed the coding algorithm needs to be introduced.

A transaction t is encoded by Krimp by searching for the first item set c in the code table for which $c \subseteq t$. The code for c becomes part of the encoding of t . If $t = c$, the algorithm continues to encode $t \setminus c$.

Since it is insisted that each code table contains at least all singleton item sets, this algorithm gives a unique encoding to each (possible) transaction over I .

The set of item sets used to encode a transaction is called its cover. Note that the coding algorithm implies that a cover consists of non-overlapping item sets.

The length of the code of an item in a code table CT depends on the database we want to compress;

the more often a code is used, the shorter it should be. To compute this code length, we encode each transaction in the database DB . The frequency of an item set $c \subseteq CT$, denoted by $\text{freq}(c)$ is the number of transactions $t \subseteq DB$ which have c in their cover. That is, $\text{freq}(c) = |\{t \subseteq DB \mid c \subseteq \text{cover}(t)\}|$. The relative frequency of $c \subseteq CT$ is the probability that c is used to encode an arbitrary $t \subseteq DB$, i.e.

$$P(c) = \text{freq}(c) / |DB|$$

For optimal compression of DB , the higher $P(c)$, the shorter its code should be. Given that we also need some code for unambiguous decoding, we use the well-known optimal Shannon code [4]:

$$|CT(c)| = \lceil \log(P(c)/|DB|) \rceil = \lceil \log \text{freq}(c) \rceil - \lceil \log |DB| \rceil$$

The length of the encoding of a transaction is simply the sum of the code lengths of the item sets in its cover. Therefore the encoded size of a transaction $t \subseteq DB$ compressed using a specified code table CT is calculated as follows:

$$|CT(t)| = \sum_{c \in \text{cover}(t; CT)} |CT(c)|$$

The size of the encoded database is the sum of the sizes of the encoded transactions, but can also be computed from the frequencies of each of the elements in the code table:

$$|CT(DB)| = \sum_{t \subseteq DB} |CT(t)|$$

$$= \sum_{c \subseteq CT} \text{freq}(c) |CT(c)| = \sum_{c \subseteq CT} \text{freq}(c) \lceil \log \text{freq}(c) \rceil - \lceil \log |DB| \rceil$$

To find the optimal code table using MDL, we need to take into account both the compressed database size (Figure 1: Krimp in action as described above, as well as the size of the code table. Over the size of the code table, we only count those item sets that have a non-zero frequency.

The size of the right-hand side column is obvious; it is simply the sum of all the different code lengths. For the size of the left-hand side column, note that the simplest valid code table consists only of the singleton item sets. This is the standard encoding (st), of which we use the codes to compute the size of the item sets in the left-hand side column. Hence, the size of code table CT is given by: $L(CT) = \sum_{c \subseteq CT} \text{freq}(c) |CT(c)|$. In [13] we defined the optimal set of (frequent) item sets as that one whose associated code table minimises the total compressed size: $L(CT) + LCT(DB)$.

Krimp starts with a valid code table (only the collection of singletons) and a sorted list of candidates (frequent item sets). These candidates are assumed to be sorted descending on 1) support size, 2) item set length and 3) lexicographically. Each candidate item set is considered by inserting it at the right position in CT and calculating the new total compressed size. A candidate is only kept in the code table if the resulting total size is smaller than it was before adding the candidate. If it is kept, all other elements of CT are reconsidered to see if they still positively contribute to compression. The whole process is illustrated in Figure 1. For more details see [13].

4 The Hypothesis for Krimp If we assume a fixed minimum support threshold for a database, Krimp has only one essential parameter:

the database. For, given the database and the (fixed) minimum support threshold, the candidate list is also specified. Hence, we will simply write CT_{DB} and $Krimp(DB)$, to denote the code table induced by Krimp from DB . Similarly CT_Q and $Krimp(Q)$ denote

the code table induced by Krimp from the result of applying query Q to DB .

Given that Krimp results in a code table, there is only one sensible way in which $Krimp(DB)$ can be re-used to compute $Krimp(Q)$: provide Krimp only with the item sets in CT_{DB} as candidates. While we change nothing to the code, we'll use the notation $Krimp_{DB}$ to indicate that Krimp got only code table elements as candidates. So, e.g., $Krimp_{DB}(Q)$ is the code table that Krimp induces from $Q(DB)$ using the item sets in CT_{DB} only.

Given our general problem statement, we have now have to prove that $Krimp_{DB}$ satisfies our two requirements for a transformed algorithm. That is, firstly, we have to show that $Krimp_{DB}(Q)$ is a good approximation of $Krimp(Q)$. That is, we have to show that $ADM(Krimp_{DB}(Q); Krimp(Q)) = |L(Krimp_{DB}(Q)) - L(Krimp(Q))| / L(Krimp(Q)) \leq \epsilon$ for some (small) epsilon. Secondly, we have to show that it is faster to compute $Krimp_{DB}(Q)$ than it is to compute $Krimp(Q)$. Given that Krimp is a heuristic algorithm, a formal proof of these two requirements is not possible. Rather, we'll report on extensive tests of these two requirements.

5 The Experiments In this section we describe our experi-

mental set-up.

First we briefly describe the data sets we used. Next we discuss the queries used for testing. Finally we describe how the tests were performed.

5.1 The Data Sets. To test our hypothesis that Krimp₊ is a good and fast approximation of Krimp, we have performed extensive test on 8 well-known UCI [3]

data sets, listed in table 1, together with their respective numbers of tuples and attributes. These data sets were chosen because they are well suited for Krimp. Some of the other data sets in the UCI repository are simply too small for Krimp to perform well. MDL needs a reasonable amount of data to be able to function.

Some other data sets are very dense. While Krimp performs well on these data sets, choosing them would have turned our extensive testing prohibitively time-consuming.

Note that all the chosen data sets are single table Dataset

#rows #attributes Heart 303 52
Iris 150 19 Led7 3200 24 Pageblocks 5473 46 Pima 786 38
Tictactoe 958 29 Wine 178 68

Table 1: UCI data sets used in the experiments.
data sets. This means, of course, that queries involving joins can not be tested in the experiments. The reason for this is simple: we have already tested the quality of Krimp₊ in earlier work [10]. The algorithm introduced in that paper, called R-Krimp, is essentially Krimp₊; we'll return to this topic in the discussion section.

5.2 The Queries To test our hypothesis, we need to consider randomly generated queries. On first sight this appears a daunting task. Firstly, because the set of all possible queries is very large. How do we determine a representative set of queries? Secondly, many of the generated queries will have no or very few results. If the query has no results, the hypothesis is vacuously true.

If the result is very small, MDL (and Krimp) doesn't perform very well.

Generating a representative set of queries with a non-trivial result set seems an almost impossible task.

Fortunately, relational query languages have a useful property: they are compositional. That is, one can combine queries to form more complex queries. In fact, all queries use small, simple, queries as building blocks.

For the relational algebra, the way to define and combine queries is through well-known operators: projection (π), selection (σ), join (\Join), union (\cup), intersection (\cap), and setminus (\setminus). As an aside, note that in principle the Cartesian product (\times) should be in the list of operators rather than the join. Cartesian products are, however, rare in practical queries since their results are often humongous and their interpretation is at best difficult. The join, in contrast, suffers less from the first disadvantage and not from the second. Hence, our omission of the Cartesian products and addition of the join.

So, rather than attempting to generate queries of arbitrary complexity, we generate simple queries only.

That is, queries involving only one of the operators π , σ , \Join , \cap , and \setminus . How the insight offered by these experiments coupled with the compositionality of relational algebra queries offers insight in our hypothesis for more general queries is discussed in the discussion section.

5.3 The Experiments The experiments performed for each of the operators on each of the data sets were generated as follows.

Projection: The projection queries were generated by randomly choosing a set X of n attributes, for $n \in \{3, 5\}$. The generated query is then π_X . For this case, the code table elements generated on the complete data set were also projected on X .

The rationale for using a small sets of attributes rather than larger ones is that these projections are the most disruptive. That is, the larger the set of attributes projected on, the more the structure of the table remains intact. Given that Krimp induces this structure, projections on small sets of attributes are the best test of our hypothesis.

Selections: The random selection queries were again generated by randomly choosing a set X of n attributes, with $n \in \{1, 2, 3, 4, 6\}$. Next for each random attribute A_i a random value v_i in its domain D_i was chosen. Finally, for each A_i in X a random $i \in \{1, 2, 3, 4, 6\}$ was chosen. The generated query is thus $\sigma_{(A_1 \times v_1) \wedge \dots \wedge (A_i \times v_i)}$.

The rationale for choosing small sets of attributes in this case is that the bigger the number of attribute sets selected on, the smaller the result of the query becomes. Too small result sets will make Krimp perform badly.

Union: For the union queries, we randomly split the dataset D in two parts D_1 and D_2 , such that $D = D_1 \cup D_2$; note that in all experiments D_1 and D_2 have roughly the same size. The random query generated is, of course, $D_1 \cup D_2$.

Krimp yields a code table on each of them, say CT_1 and CT_2 . To test the hypothesis, we give Krimp₊ the union of the item sets in CT_1 and CT_2 .

In practice, tables that are combined using a union may not be disjoint. To test what happens with various level of overlap between D_1 and D_2 , we tested at overlap levels from 0%; 33.3%; 50%.

Intersection: For the intersection queries, we again randomly split the data set D into two overlapping parts D_1 and D_2 . Again, such that $D = D_1 \cup D_2$ and again in all experiments D_1 and D_2 have roughly the same size. The random query generated is, of course, $D_1 \cap D_2$.

Again Krimp yields a code table on each of them, say CT_1 and CT_2 . To test the hypothesis, we give Krimp₊ the union of the item sets in CT_1 and CT_2 .

The union of the two is given as either of one might expect good codes for the intersection. The small raise in the number of candidates is offset by this potential gain.

In this case the overlap levels tested were from f33:3%; 50%; 66:6%.

Selection queries can, of course, be seen as a kind of setminus queries. They are special, though, in the sense that they remove a well described part of the data.

For less well structured setminus operations, we simply generated random subsets of the data set. The sizes of these subsets are chosen from f33:3%; 50%; 66:6%.

Each of these experiments is performed ten times on each data set.

Results In this section we give an overview of the results of the experiments described in the previous section. The relational algebra operator is briefly discussed in the next section.

Projection The projection results are given in Table 2. The ADM scores listed are the average ADM score over 10 projection experiments performed on that data set. The standard deviation of those 10 ADM scores. Similarly, the Size scores. Note that Size stands for the reduction in the number of candidates.

A Size score of 0.2, means that Krimp got only 20% of the number of candidates that Krimp got for the original result.

Notice that most of the ADM scores are in the range 0.1 to 0.2, whereas the Size scores are generally lower. The notable exceptions are the scores for the Heart and, in one case, for Led7. Note, however, that these are averages, the standard deviation is generally high. As one would expect, this is caused by a few outliers. That is, if one looks at the individual scores, one or two are very high. Random experiments have their disadvantages.

However, one should note, however, that these figures are for randomly selected sets of attributes. Such projections are about as disruptive of the data as possible. In other words, it is impressive that Krimp manages to do so well.

One can see that, e.g., by comparing the results for the same data set for projections on 3 and 5 attributes. Clearly, these differences are in the trend and the trend doesn't always hold. We will also see in the other experiments.

The selection results are given in Table 3. The ADM scores are the averages. The standard deviation is also given. The resulting ADM scores are now in the range of just a few percent. This is all the better when one considers the Size scores.

The Size scores were reached while Krimp got 2% of the number of candidates than the original result. It got less than 1% of the num-

ber of candidates.

The fact that Krimp performs so well for selections means that while Krimp models the global underlying data distribution, it still manages capture the "local" structure very well. That is, if there is a pattern that is important for a part of the database, it will be present in the code table.

The fact that the results improve with the number of attributes in the selection, though mostly not significantly, is slightly puzzling. If one looks at all the experiments in detail, the general picture is that bigger query results give better results. In this table, this global picture seems reversed. We do not have a good explanation for this observation.

6.3 Union The projection results are given in Table 4. The general picture is very much as with the previous experiments. The ADM score is a few percent, while the reduction in the number of candidates is often impressive.

The notable exception is the Iris database. The explanation is that this data set has some very local structure that (because of minsup settings) doesn't get picked up in the two components; it only becomes apparent in the union. Note that this problem is exaggerated by the fact that we split the data sets at random. The same explanation very much holds for the first Led7 experiment.

We already alluded a few times to the general trend that the bigger the query results, the better the results.

This trend seems very apparent in this table. For, the higher the overlap between the two data sets, the bigger the two sets are, since their union is the full data set.

However, one should note that this is a bit misleading, for the bigger the overlap the more the two code tables "know" about the "other" data distribution.

6.4 Intersection The projection results are given in Table 5. Like with for the union, the reduction of the number of candidates is again huge in general. The ADM scores are less good than for the union, however, still mostly below 0.1. This time the Heart and the Led7 databases that are the outliers. Heart shows the biggest reduction in the number of candidates, but at the detriment of the ADM score. The explanation for these relative bad scores lies again in local structures, that have enough support in one or both of the components, but not in the intersection. That is, Krimp doesn't see the good candidates for the tuples that adhere to such local structures. This is witnessed by the fact that some tuples are compressed better by the original code tables than by the Krimp generated code table for the intersection. Again, this problem is, in part, caused by the fact that we split our data sets at random.

The ADM scores for the other data sets are more in line with the numbers we have seen before. For these, the ADM score is below 0.2 or (much) lower.

6.5 Setminus The projection results are given in Table 6.

Both the ADM scores and the Size scores are very good for all of these experiments. This does make sense, each of these experiments is computed on a random subset of the data. If Krimp is any good, the code tables generated from the complete data set should compress a random subset well.

It may seem counter intuitive that the ADM score grows when the size of the random subset grows. In fact, it is not. The bigger the random subset, the closer its underlying distribution gets to the "true" underlying distribution. That is, to the distribution that underlies the complete data set. Since Krimp has seen the whole data set, it will pick up this distribution better than Krimp_{sub}.

7 Discussion

First we discuss briefly the results of the experiments. Next we discuss the join. Finally we discuss what these experiments mean for more general queries.

7.1 Interpreting the Results

The Size scores re-reported in the previous section are easy to interpret.

They simply indicate how much smaller the candidate set becomes. As explained before, the runtime complexity of Krimp is linear in the number of candidates. So, since the Size score is never below 0.4 and, often, considerably lower, we have established our first goal for Krimp_{sub}. It is faster, and often far faster, than Krimp.

In fact, one should also note that for Krimp_{sub}, we do not have to run a frequent item set miner. In other words, in practice, using Krimp_{sub} is even faster than suggested by the Size scores.

But, how about the other goal: how good is the approximation? That is, how should one interpret ADM scores? Except for some outliers, ADM scores are below 0.2. That is, a full-edged Krimp run compresses the data set 20% better than Krimp_{sub}. Is that good?

In a previous paper [15], we took two random samples from data sets, say D1 and D2. Code tables CT1 and CT2 were induced from D1 and D2 respectively.

Next we tested how well CT1 compressed D2. For the four data sets also used in this paper, Iris, Led7, Pima and, PageBlocks, the "other" code table compressed 16% to 18% worse than the "own" code table; the figures for other data sets are in the same ballpark. In other words, an ADM score on these data sets below 0.2 is on the level of "natural variations" of the data distribution. Hence, given that the average ADM scores are often much lower we conclude that the approximation by Krimp_{sub} is good.

In other words, the experiments verify our hypothesis: Krimp_{sub} gives a fast and good approximation of Krimp. At least for simple queries.

7.2 The Join

In the experiments, we did not test the join operator. We did, however, already test the join in a previous paper [10]. The R-Krimp algorithm introduced in that

paper is Krimp_{sub} for joins only.

Given two tables, T1 and T2, the code table is induced on both, resulting in CT1 and CT2. To compute the code table on T1 on T2, R-Krimp only uses the item sets in CT1 and CT2. Rather than using, the union of these two sets, for the join one uses pairs (p1; p2), with p1 \subseteq CT1 and p2 \subseteq CT2.

While the ADM scores are not reported in that paper, they can be estimated from the numbers reported there. For various joins on, e.g., the well known financial data set, the ADM can be estimated as to be between 0.01 and 0.05. The Size ranges from 0.3 to 0.001; see [10] for details.

In other words, Krimp_{sub} also achieves its goals for the join operator.

7.3 Complex Queries

For simple queries we know that Krimp_{sub} delivers a fast and good approximation. How about more complex queries?

As noted before, these complex queries are built from simpler ones using the relational algebra operators.

Hence, we can use error propagation to estimate the error of such complex queries.

The basic problem is, thus, how do the approximation errors propagate through the operators? While we do have no definite theory, at worst, the errors will have to be summed. That is, the error of the join of two selections will be the sum of the errors of the join plus the errors of the selections.

Given that complex queries will only be posed on large database, on which krimp performs well. The initial errors will be small. Hence, we expect that the error on complex queries will still be reasonable; this is, however, subject to further research.

8 Related Work

While there are, as far as the authors know, no other papers that study the same problem, the topic of this paper falls in the broad class of data mining with background knowledge. For, the model on the database, MDB, is used as background knowledge in computing MQ. While a survey of this area is beyond the scope of this paper, we point out some papers that are related to one of the two aspects we are interested in, viz., speed-up and approximation.

A popular area of research in using background knowledge is that of constraints. Rather than trying to speed up the mining, the goal is often to produce models that adhere to the background knowledge. Examples are the use of constraints in frequent pattern mining, e.g. [2], and monotonicity constraints [6]. Note, however, that for frequent pattern mining the computation can be speeded up considerably if the constraints can be pushed into the mining algorithm [2]. So, speed-up is certainly a concern in this area. However, as far

as we know approximation plays no role. The goal is still to find all patterns that satisfy the constraints.

Another use of background knowledge is to find un-explained patterns. In [9], e.g., Bayesian Networks of the data are used to estimate how surprising a frequent pattern is. In other words, the (automatically induced) background knowledge is used to filter the output. In other words, speed-of-computation is not a concern in this approach. Ap-proximation clearly works in the opposite direction of ours: the more a pattern deviates from the global model, the more interesting it becomes. Whereas we would like that all patterns in the answer are covered by our approximate answer. 9 In this paper we introduce a new problem: given that we have a model induced from a database DB, how can we use it in inducing a model on the result of a query Q on DB. For a given mining algorithm A, we formalize this problem as the construction of an algorithm A' such that:

(1) A' gives a reasonable approximation of A when applied to the result of Q on DB, (2) A' is faster to compute than MQ.

(3) A' is faster to compute than MQ.

We formalize the approximation in the first point using

the following definition for this problem for a particular algorithm A. The reason for using Krimp as our problem is twofold. Firstly, from earlier research we know that Krimp characterizes the underlying data distribution well, see, e.g., [10]. Secondly, from earlier research on Krimp in a multi-dimensional setting, we already know that Krimp is easily interpretable [10]. Finally, Krimp is MDL based, which makes it a good fit for the problem as formalised.

The mining algorithm is Krimp, which is actually the algorithm that gets a restricted input.

On a set of data sets and many different queries, we show that Krimp yields fast and good approximations.

Complex queries are currently under

research.

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Dataset 3 attr 5 attr ADM Size ADM Size
Heart 0.06_0.09 0.2_0.13 0.03_0.03 0.2_0.13
Iris 0.24_0.28 0.17_0.12 0.21_0.18 0.14_0.12
Led7 0.05_0.1 0.31_0.23 0.38_0.34 0.25_0.19
PageBlocks 0.04_0.06 0.23_0.21 0.08_0.06 0.2_0.17
Pima 0.04_0.05 0.14_0.13 0.08_0.07 0.23_0.17
TicTacToe 0.12_0.09 0.11_0.17 0.09_0.1 0.17_0.11
Wine 0.16_0.2 0.10_0.09 0.1_0.11 0.1_0.09

Table 2: The results of the projection experiments. The ADM and Size scores are averages _ standard deviation

Dataset 1 attr 2 attr 3 attr 4 attr
ADM Size ADM Size ADM Size ADM Size
Heart 0.04_0.03 0.04_0.11 0.04_0.03 0.02_0.002 0.04_0.03 0.003_0.003 0.02_0.02 0.001_0.0004
Iris 0.04_0.04 0.09_0.01 0.05_0.05 0.1_0.02 0.04_0.01 0.1_0.01 0.01_0.03 0.1_0.01
Led7 0.04_0.06 0.02_0.001 0.04_0.01 0.02_0.001 0.03_0.02 0.02_0.001 0.03_0.03 0.02_0.01
PageBlocks 0.09_0.07 0.007_0.008 0.05_0.04 0.002_0.0002 0.03_0.02 0.002_0.0002 0.02_0.02 0.002_0.0002
Pima 0.1_0.14 0.01_0.003 0.03_0.02 0.01_0.003 0.03_0.02 0.01_0.002 0.03_0.02 0.01_0.001
TicTacToe 0.16_0.09 0.01_0.002 0.1_0.028 0.01_0.002 0.12_0.04 0.02_0.02 0.08_0.03 0.01_0.005
Wine 0.03_0.03 0.02_0.02 0.02_0.02 0.02_0.02 0.02_0.02 0.01_0.01 0.006_0.02 0.01_0.01 0.005

Table 3: The results of the selection experiments. The ADM and Size scores are averages _ standard deviation

Dataset 0% 33.3% 50%
ADM Size ADM Size ADM Size
Heart 0.07_0.02 0.0001_0.0001 0.04_0.02 0.001_0.00004 0.03_0.05 0.001_0.0002
Iris 0.36_0.11 0.07_0.01 0.37_0.1 0.07_0.007 0.34_0.12 0.07_0.006
Led7 0.38_0.31 0.02_0.005 0.05_0.02 0.03_0.002 0.03_0.02 0.03_0.002
PageBlocks 0.06_0.01 0.002_0.0001 0.04_0.01 0.003_0.0001 0.02_0.01 0.003_0.0001
Pima 0.04_0.03 0.01_0.0006 0.03_0.02 0.02_0.002 0.03_0.02 0.02_0.002
TicTacToe 0.07_0.01 0.009_0.0005 0.03_0.02 0.01_0.0003 0.01_0.002 0.01_0.0002
Wine 0.03_0.01 0.006_0.0003 0.03_0.01 0.008_0.0006 0.02_0.01 0.008_0.0003

Table 4: The results of the union experiments. The percentages denote the amount of overlap between the two data sets. The ADM and Size scores are averages _ standard deviation

Dataset 33.3% 50% 66.6%
ADM Size ADM Size ADM Size
Heart 0.39_0.14 0.0002_0.0001 0.36_0.05 0.0002_0.0001 0.42_0.17 0.0001_0.0001
Iris 0.09_0.08 0.1_0.02 0.08_0.07 0.09_0.02 0.03_0.01 0.09_0.01
Led7 0.5_0.14 0.005_0.002 0.42_0.1 0.007_0.001 0.12 0.01_0.001
PageBlocks 0.13_0.07 0.001_0.0002 0.09_0.06 0.001_0.0001 0.07_0.05 0.002_0.0001
Pima 0.09_0.06 0.01_0.002 0.09_0.09 0.01_0.003 0.06 0.01_0.002
TicTacToe 0.2_0.05 0.007_0.002 0.22_0.04 0.005_0.002 0.24_0.04 0.004_0.0007
Wine 0.1_0.02 0.01_0.005 0.12_0.03 0.005_0.0001 0.04 0.002_0.0006

Table 5: The results of the intersection experiments. The percentages denote the amount of overlap between the two data sets. The ADM and Size scores are averages _ standard deviation

Dataset 33.3% 50% 66.6%
ADM Size ADM Size ADM Size
heart 0.01_0.01 0.001_0.00007 0.01_0.01 0.001_0.0003 0.02 0.002_0.0004
iris 0.003_0.006 0.11_0.007 0.005_0.008 0.12_0.02 0.14_0.01
led7 0.02_0.02 0.02_0.0002 0.02_0.02 0.02_0.0003 0.02_0.001
pageBlocks 0.01_0.004 0.002_0.00004 0.02_0.00003 0.03_0.01 0.003_0.00007
pima 0.02_0.01 0.02_0.001 0.01_0.01 0.01 0.02_0.002 0.02_0.001
ticTacToe 0.06_0.02 0.01_0.0003 0.07_0.02 0.01_0.008 0.02 0.02_0.002
wine 0.01_0.007 0.01_0.002 0.02_0.01 0.02_0.02 0.04_0.01

Table 6: The results of the setminus experiments. The percentages denote the size of the remaining data set. The ADM and Size scores are averages _ standard deviation